

ANALYSIS OF ADAPTIVE NEURO-FUZZY INFERENCE SYSTEM FOR THE PREDICTION OF HYBRID COMPOSITES

C. KAVITHA¹, T. S. FRANK GLADSON, AND M. PRASANNA JEYANTHI

ABSTRACT. In this paper, prediction of surface roughness is evaluated using ANFIS [Adaptive Neuro-Fuzzy Inference System] methodology for the cutting parameters of end-milling process for machining the halloysite nano tubes (HNTs) with aluminium reinforced epoxy hybrid composite material. Experimental data are used to analyze the relationship between the input parameter such as depth of cut (d), cutting speed (S), feed-rate (f) and output parameters as surface roughness. ANFIS maps input, output parameter through membership functions. Fuzzy inference system (FIS) will generate the membership function by grid partition and sub clustering methods. To train the FIS several optimization routines could be applied in order to adjust the parameters and to reduce the sum of the squared errors. Optimization method is a combination of hybrid and backpropagation is adopted. Data are classified into training and testing with different types of membership functions. The observed results accurately predict the output which was not used in training and it is almost very close to the actual output obtained in the experimental work. Moreover it was found that gbellmf is helpful for better prediction with minimum error.

1. INTRODUCTION

Surface roughness plays a vital role in manufacturing field. It influences the mechanical properties, cost and quality of a product. Research activities are

¹corresponding author

2010 *Mathematics Subject Classification.* 03B52, 90C70.

Key words and phrases. ANFIS, Hallosyite nanotubes, Surface roughness, depth of cut, cutting speed and feed rate.

involved to decrease the surface roughness by varying many types of hybrid composition of materials, there are many statistical tools to find the influence parameter, optimizing the parameter and tools to predict the output without doing many experimental data.

I.El-Sonbaty et.al [2] obtained Polymer composite products by primary manufacturing process and secondary manufacturing process. Secondary process involves drilling and saw cutting. Drilling is employed to make bolted or riveted assemblies and defects like delamination, crack, undesired hole surface roughness related to tool wear encountered. Sheet molding compound composite was drilled under different cutting speed, feed and drill point angles. R.C.L.Dutra et.al [3] investigate the influence of parameters such as cutting speed, feed, drill size, fiber volume fraction on the thrust force, torque and surface roughness in drilling processes of fiber-reinforced composite materials. They found that Drill diameter combined with feed has a significant effect on surface roughness. Moon II Kim et.al [4] proposed Hybrid composites containing Polypropylene fiber and mercapto-modified polypropylene blend fibers display higher impact strength than plain carbon fiber composites but the performance is lower than plain Polypropylene fiber and mercapto-modified polypropylene epoxy composite. Minggang Dong et.al [5] found that Zirconium oxide-impregnated halloysite nano tubes were added to epoxy resins to obtain epoxy composites with improved mechanical, thermal and flexural properties. Alper Uysal et.al [1] improve the prediction of surface roughness in end milling process by ANFIS and leave-one-out cross-validation (LOO-CV) approach. In this paper, cutting parameters of end-milling process for machining the halloysite nano tubes (HNTs) with aluminium reinforced epoxy hybrid composite material is modeled using adaptive neuro fuzzy inference system.

2. METHODOLOGY - ADAPTIVE NEURO FUZZY INFERENCE SYSTEM (ANFIS) METHOD

ANFIS methodology was proposed by Jang [9] in 1993. Geoffrey Boothroyd et.al [6] proposed ANFIS as a hybrid combination of two methods such as Adaptive Neural Network (ANN) and Takagi-Sugeno Fuzzy Inference system. Fuzzy logic is implemented in Neural network to construct an input-output mapping for the associated parameters through input, output membership functions

based on human knowledge in the form of Fuzzy Inference System (FIS) followed by IF-THEN rules to determine the optimal distribution of membership functions. Neural networks are used to train and test the input-output data by back-propagation, gradient descent, least squares method by reducing the sum of the squared errors to predicate the output. Architecture of the ANFIS structure and schematic structure of ANFIS network in each layer is represented in Fig. 1 and Fig.2.

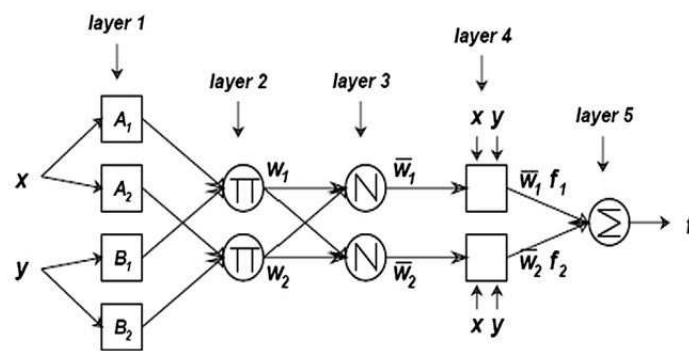


FIGURE 1. Architecture of ANFIS structure

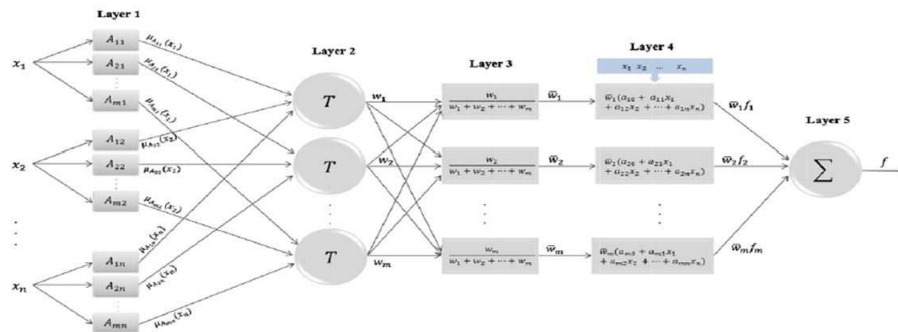


FIGURE 2. Schematic structure of ANFIS network

P.M. Pradhan et.al [7] investigated as ANFIS consist of five network layers used to create fuzzy inference system. Every layer has different function such as Fuzzy layer, Product layer, Normalized layer, Defuzzify layer and Output layer. Layer consists of two different types of nodes such as squares and circles. Square nodes are adaptive nodes where the factors could be changed and the circles

are fixed nodes where the factors are fixed whose parameters change during the training process. Muhammad Rizal et.al [8] used Input nodes to represent the training values, output nodes represent predicted values and in hidden layers there are nodes functioning as membership functions and rules. The present layers' inputs are derived from the nodes in the previous layers. The rule base of ANFIS contains fuzzy IF-THEN rules of the Sugeno type. For a first-order Sugeno fuzzy inference system, the two rules may be stated as:

Rule 1 IF x is A_1 AND y is B_1 , THEN f is $f_1(x, y)$

Rule 2 IF x is A_2 AND y is B_2 , THEN f is $f_2(x, y)$

where x and y are the inputs of ANFIS, A_i and B_i are the fuzzy sets, and $f_i(x, y) = p_i x + q_i y + r_i$, p_i, q_i, r_i are design parameters that are determined during the training process, f_i is a first order polynomial and represents the outputs of the first order Sugeno fuzzy inference system. Jang J used to Characteristics of each layer in ANFIS described as below:

Layer 1 Fuzzy layer has adaptive nodes with node function which converts the inputs into linguistic labels to calculate membership values of the data. The output of these layer nodes is membership value of input in following structure:

$$\begin{aligned} O_{1,i} &= \mu_{A_i}(x_1), \quad \text{for node } i=1, 2, \\ O_{1,i} &= \mu_{B_{i-2}}(x_2), \quad \text{for node } i=3, 4. \end{aligned}$$

where x_1 and x_2 are the input to node i , A_i B_{i-2} are fuzzy sets which contains linguistic terms such as small, large etc. $\mu_{A_i}(x_1)$ and $\mu_{B_{i-2}}(x_2)$ are the membership functions. Membership functions are different types such as triangular, trapezoidal, generalized bell shaped, gaussian curve, gaussian combination, Π -shaped, difference between two sigmoidal and product of two sigmoidal membership functions are used to represent the linguistic terms.

Layer 2 Product layer has fixed nodes, it is marked by a circle, and it is labeled as Π . The output of each node function has to be multiplied by input signals from the previous layer. The nodes of this layer are called rule nodes and it computes the firing strength of the associated rule.

$$O_{2,i} = w_i = \mu_{A_i}(x_1)\mu_{B_i}(x_2), \quad \text{for node } i=1, 2.$$

Layer 3 Normalized layer has fixed nodes, marked by a circle and labeled by N . The i^{th} node of this layer calculates the normalized firing strength as ratio of

i^{th} node firing strength to the sum of all rules firing strengths. Output of the i^{th} node of this layer can be represented as

$$O_{3,i} = \bar{w} = \frac{w_i}{w_1 + w_2} \quad \text{for node } i=1, 2.$$

Layer 4 Defuzzify layer has adaptive nodes, marked by a square and labeled by D. This layer computes the product of normalized firing strength and first order polynomial [sugeno model]. Takagi-sugeno type output of this layer can be represented as

$$O_{4,i} = \bar{w}_i f_i = \bar{w}_i (p_i x_1 + q_i x_2 + r_i).$$

where the evaluation of right hand side polynomials perform consequent parameters as $\{p_i, q_i, r_i\}$, $\bar{w}_i$ is the normalized weighting factor of the i^{th} rule, f_i is the output of the i^{th} rule of this node.

Layer 5 Output layer has fixed node marked by a circle and labeled by Σ . This layer computes the overall output as the summation of all incoming signals

$$O_{5,i} = \bar{w}_i f_i = \frac{\sum_i w_i f_i}{\sum_i w_i}.$$

Hybrid learning algorithm is used to increase the convergence rate and it is used to update the premise parameters by integrating the least square and gradient descent method. To optimize the consequent parameters least square method is employed and to optimize the premise parameters gradient descent method is used Ilhan Asilturk et.al [10]. Total output of ANFIS is determined by consequent parameters p, r, q and is given by the following equation

$$O_{5,i} = \frac{w_1}{w_1 + w_2} f_1 + \frac{w_2}{w_1 + w_2} f_2.$$

$$i.e., O_{5,i} = \bar{w}_1 (p_1 x_1 + q_1 x_2 + r_1) + \bar{w}_2 (p_2 x_1 + q_2 x_2 + r_2).$$

3. RESULTS AND DISCUSSION - PREDICTION OF SURFACE ROUGHNESS BY ANFIS

ANFIS methodology is used to predict surface roughness for the cutting parameters of end-milling process for machining the halloysite nanotubes (HNTs) with aluminium reinforced epoxy hybrid composite material. In this study, data has been extracted from J.S.Pang et.al [11] and shown in Table 1. Inputs are machining parameters such as depth of cut (d)(mm), cutting speed (S)(rpm),

Record	Input 1 (d)	Input 2 (S)	Input 3 (f)	Output (Ra)
1	0.4	500	20	1.15
2	0.4	500	60	1.18
3	0.4	1000	20	0.96
4	0.4	1000	40	0.62
5	0.4	1500	40	0.36
6	0.4	1500	60	0.29
7	0.6	500	20	1.43
8	0.6	500	40	0.89
9	0.6	1000	40	0.86
10	0.6	1000	60	0.77
11	0.6	1500	20	0.37
12	0.6	1500	60	0.84
13	0.8	500	40	1.8
14	0.8	500	60	1.81
15	0.8	1000	20	1.15
16	0.8	1000	60	2.11
17	0.8	1500	40	1.25
18	0.8	1500	20	0.95

TABLE 1. Data used in present paper (J.S.Pang et.al [11])

Record	Input 1 (d)	Input 2 (S)	Input 3 (f)	Output (Ra)
1	0.4	500	40	1.94
2	0.4	1000	60	0.77
3	0.4	1500	20	1.06
4	0.6	500	60	1.28
5	0.6	1000	20	1.1
6	0.6	1500	40	0.63
7	0.8	500	20	1.14
8	0.8	1000	40	1.43
9	0.8	1500	60	0.47

TABLE 2. Testing datasets for ANFIS model

No	No. of Memb. func.	Function Type	Output Function	Error (RMSE)	
				Training Error	Testing Error
1	3 3 3	Trimf	Constant	1.1547×10^{-6}	1.1686
			Linear	6.3513×10^{-5}	1.1686
2	3 3 3	trapmf	Constant	1.1548×10^{-6}	1.1686
			Linear	6.5701×10^{-5}	1.1686
3	3 3 3	gbellmf	Constant	1.3184×10^{-6}	0.88744
			Linear	0.00020792	0.76018
4	3 3 3	Gaussmf	Constant	1.3189×10^{-6}	0.92096
			Linear	0.00018292	0.7779
5	3 3 3	Gauss2mf	Constant	1.1554×10^{-6}	1.1675
			Linear	0.00021836	1.1668
6	3 3 3	pimf	Constant	1.1548×10^{-6}	1.1686
			Linear	6.5701×10^{-6}	1.1686
7	3 3 3	dsigmf	Constant	1.1558×10^{-6}	1.1665
			Linear	0.0002129	1.1638
8	3 3 3	psigmf	Constant	1.1555×10^{-6}	1.167
			Linear	0.0001983	1.1457

TABLE 3. Comparing the result of different membership functions using hybrid method

feed rate (f)(mm/pm) and the outputs are the surface roughness (Ra)(μm) of the machined composite surface .

ANFIS methodology is solved by Neuro fuzzy designer in MATLAB toolbox, which applies fuzzy inference techniques to data modeling using a graphical user interface. Initially data are trained in ANFIS using existing input / output training data set. Based on the training data it constructs Sugeno-type fuzzy inference system (FIS) whose parameters are tuned to membership function. In this paper, Membership functions associated with the input / output parameters changes through the learning process and the adjustment of these parameters is done by a gradient vector such as grid partition and sub clustering. Optimization method is used to adjust the parameters to reduce some error measure by sum of the squared difference between actual and desired outputs. In this paper, Data which are trained by FIS uses optimization method such as backpropagation and

combination with a least square method for membership function parameter estimation. The training process continues till the desired number of training steps (epochs) or the desired root mean squared error (RMSE) between the desired and the generated output is achieved. If the training process over then the testing data will be used in the same manner to test the generalization ability of tuned system and achieve the desire output.

Input data set for training / testing process are machining parameters such as depth of cut (d) (mm), cutting speed (S) (rpm) and feed rate (f) (mmpm) is in Table 1 and Table 2.

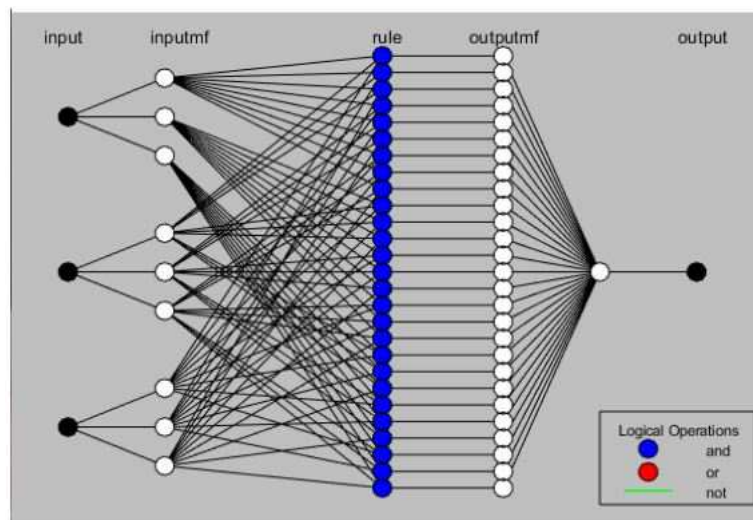


FIGURE 3. ANFIS Structure based on grid partition

- Step 1 The ANFIS model is employed to train the data set in table 1. ANFIS uses multi input single output structure. It maps input through input membership function and output through output membership function. Parameters associated with each membership function keep changing throughout the learning process.
- Step 2 Grid partition technique is used to generate membership function for the parameters and to generate the optimized rules of a given dataset using sugeno-type fuzzy inference system.
- Step 3 Optimized rules use hybrid learning by combining the gradient descent and the least square method. ANFIS structure to predict surface roughness based on grid partition is in figure 3.

- Step 4 The input dataset is plotted several times to reduce the prediction error in the training process. To achieve minimal error in parameters best learning procedure is adapted in ANFIS. Numbers of iterations in training process are stated as Epochs and by conducting more number of experiments it reach the optimal number of epoch. Number of experiments done in the paper is 18 and to determine the optimal epoch number with the lowest RMSE, number of iteration required is 100 epochs.
- Step 5 The predictive competence of the corresponding model is tested with the testing data in Table 2. To validate the model, 9 data are tested after the training process. Training and testing data parameters are validate with different type of membership functions to get the output in the form of linear, constant using hybrid optimization method is in Table 3. Similarly the same set of training and testing data parameters are validate with different type of membership functions to get the output in the form of linear, constant using backpropagation method is in Table 4. Membership function uses three linguistic variables to get the best optimal ANFIS structure. Using hybrid optimization method, gbell membership functions in comparison with the other membership functions which have low prediction error. i.e. RMSE for training is 1.3184×10^{-6} and for testing is 0.88744 . Using backpropagation method, dsigmf and psigmf membership function for constant with other membership function have low prediction error. i.e. RMSE for training is 0.0019694 and for testing is 1.1664 . Using backpropagation method, Gaussmf and gbellmf membership function for linear with other membership function have low prediction error. i.e. RMSE Gaussmf for training is 1.6777and for testing is 0.81124, RMSE gbellmf for training is 1.6988and for testing is 0.76592.
- Step 6 Generate fuzzy inference system structure using subtractive clustering. It is used to generate an initial FIS for anfis training by extracting a set of rules, antecedent membership functions and uses linear least squares estimation to determine each rule consequent equations. All the membership functions used in the chosen neuro-fuzzy system were Gaussians. Squash factor find clusters that are far from each other. Default positive scalar is 1.25. It is used for scaling the range of influence of cluster centers. A smaller squash factor reduces the potential for outlying points

No	No. of Memb.func.	Function Type	Output Function	Error (RMSE	
				Training Error	Testing Error
1	3 3 3	Trimf	Constant Linear	0.0021725 1.98	1.1686 1.1531
2	3 3 3	trapmf	Constant Linear	0.0021718 1.9794	1.1686 1.686
3	3 3 3	gbellmf	Constant Linear	0.31319 1.6988	0.42573 0.76592
4	3 3 3	Gaussmf	Constant Linear	0.29105 1.6777	0.4545 0.81124
5	3 3 3	Gauss2mf	Constant Linear	0.0022002 1.9781	1.1674 1.1658
6	3 3 3	pimf	Constant Linear	0.0021718 1.9794	1.1686 1.1686
7	3 3 3	dsigmf	Constant Linear	0.0019694 1.7098	1.1664 0.96399
8	3 3 3	psigmf	Constant Linear	0.0019694 1.71	1.1664 1.0937

TABLE 4. Comparing the result of different membership functions using backpropagation method

No	Fuzzy inference System	Train FIS Optim Method	Error (RMSE			
			Training Error	Epoche	Testing Error	Epoches
1	Sub clustering	Hybrid	0.00028305	300	0.58913	300
2	Sub clustering	Backprop.	2.4253	300	1.7018	300

TABLE 5. Comparing the result to generate FIS using Sub clustering and Train FIS using Hybrid and backpropagation method

Range of influence	Squash factor	Accept ratio	Reject ratio
0.5	1.25	0.5	0.15

TABLE 6. Default Scalar value in subtractive clustering

to be a part of a cluster. Accept data points with a strong potential for being cluster centers. Default value is 0.5 and Scalar value in the range [0, 1]. Acceptance ratio must be greater than the rejection ratio. Reject ratio reject data points if they do not have a strong potential for being cluster centers. Default value is 0.15 and scalar value in the range [0,1]. Rejection ratio must be less than acceptance ratio. Generation of FIS using subclustering and train by hybrid, backpropagation is shown in Table 5. Table 6 shows the default scalar value of subtractive clustering.

4. CONCLUSION

Adaptive neuro-fuzzy inference system constructs a fuzzy inference system for a given input / output data set whose membership function parameters are adjusted using a back propagation algorithm or in combination with a least squares type of method.. The ANFIS model has been attempted for predicting surface roughness of the cutting parameters of end-milling process for machining the halloysite nanotubes (HNTs) with aluminium reinforced epoxy hybrid composite material. Experimental values are compared with predicted values of ANFIS and it is found that it is accurate. ANFIS model is checked with different types of membership function with constant and linear type. In that ANFIS model with gbellmf membership function is selected as best based on the minimum RSME prediction error of about 1.3184×10^{-6} . It is found that the ANFIS method can be able to attain a better prediction model of the experimental values.

REFERENCES

- [1] A. UYSAL, M. ALFAN, E. ALTAN: *Effects of cutting parameters on tool wear in drilling of polymer composite by taguchi method*, International Journal of Advance Manufacturing Technology, **58**(2012), 915-921. DOI 10.1007/S00170-011-3464-6.
- [2] I. EL-SONBATY, U. A. KHASHABA, T. MACHALY: *Factors affecting the machinability of GFR/epoxy composites*, Composite Structures, **63**(3-4) (2004), 329-338. DOI 10.1016/S0263-8223(03)00181-8.
- [3] R. C. L. DUTRA, B. G. SOARES, E. A. CAMPOS, J. L. G .SILVA: *Hybrid composites based on polypropylene and carbon fiber and epoxy matrix*, Polymer, **41**(10) (2000), 3841-3849. DOI 10.1016 / S0032-3861(99)00552-2.

- [4] M. I. KIM, S. KIM, T. KIM, D. K. LEE, B. SEO, C. LIM: *Mechanical and Thermal properties of Epoxy composites containing Zirconium oxide Impregnated Halloysite nanotubes*, Coatings, **7**(12) (2017), 231. DOI 10.3390/coatings7120231.
- [5] M. DONG, N. WANG: *Adaptive network-based fuzzy inference system with leave-one-out cross-validation approach for prediction of surface roughness*, Applied Mathematical Modelling, **35** (2011), 1024-1035. DOI: 10.1016/j.apm.2010.07.048.
- [6] G. BOOTHROYD, W. A. KNIGHT: *Fundamentals of Machining and Machine tools*, (Marcel Dekker Inc., New York) (Second Edition), 1989.
- [7] P. M. PRADHAN, Y. ALKASSAR, P. K. MAHTO, R. GHADAI: *Prediction of Surface Roughness for different angle bends in Pneumatic Conveying System using Regression Analysis and ANFIS*, BLB- International Journal of Science and Technology, (2015) 359-365.
- [8] M. RIZAL, J. A. GHANI, M. Z. NUAWI, C. HARON : *Hybrid composites based on polypropylene and carbon fiber and epoxy matrix Online tool wear prediction system in the turning process using an adaptive neuro-fuzzy inference system*, Applied Soft Computing, **13** (2013), 1960-1968.
- [9] J. JANG: *ANFIS: adaptive-network-based fuzzy inference system*, IEEE Trans Syst Man Cybern, **23** (1993), 665-85.
- [10] I. ASILTURK, M. TINKIR, H. EL MONUAYRI, L. CELIK : *An intelligent system approach for surface roughness and vibrations prediction in cylindrical grinding*, International Journal of Computer Integrated Manufacturing, **25** (2012), 750-759. DOI: 10.1080/0951192X.2012.665185.
- [11] J. S. PANG, M. N. M. ANSARI, O. S. ZAROOG, M. H. ALI, S. M. SAPUAN : *Taguchi design optimization of machining parameters on the CNC end milling process of halloysite nanotube with aluminium reinforced epoxy matrix (HNT/Al/Ep) hybrid composite*, HBRC Journal, **10** (2014), 138-144. DOI:10.1016/j.hbrj.2013.09.007

DEPARTMENT OF MATHEMATICS

SATHYABAMA INSTITUTE OF SCIENCE AND TECHNOLOGY, CHENNAI

E-mail address: ckavitha.maths@sathyabama.ac.in

DEPARTMENT OF MECHANICAL ENGINEERING

VELAMMAL ENGINEERING COLLEGE, SURAPET, CHENNAI

E-mail address: frankgladson@velammal.edu.in

DEPARTMENT OF MATHEMATICS

SATHYABAMA INSTITUTE OF SCIENCE AND TECHNOLOGY, CHENNAI

E-mail address: prasannajeyanthi@gmail.com